

Some discussion/confusion about wave physics

In a nutshell

$$y(x,t) = \sum \sin \frac{n\pi x}{L} \left(a_n \cos \frac{n\pi v t}{L} + b_n \sin \frac{n\pi v t}{L} \right)$$

↑
↑
↑
 spatial temporal

$$v = \sqrt{\frac{T}{\mu}}$$

Q: why does temporal "wave function depend on physical parameters but not the spatial wf?" Esp since wave eqn is relativistically covariant (unlike Schr Eqn)

Pot another way: Separate variables $y(x,t) = f(x)g(t)$

$$\frac{1}{f} \frac{d^2 f}{dx^2} = -k^2 = \frac{1}{v^2} \frac{d^2 g}{dt^2}$$

$$f(x) = \begin{matrix} \cos kx \\ \sin kx \end{matrix} \quad g(t) = \begin{matrix} \cos vkt \\ \sin vkt \end{matrix}$$

$$v^2 \frac{1}{f} \frac{d^2 f}{dx^2} = -\omega^2 = \frac{d^2 g}{dt^2}$$

$$\begin{matrix} \cos \omega/v x \\ \sin \omega/v x \end{matrix}$$

$$\begin{matrix} \cos \omega t \\ \sin \omega t \end{matrix}$$

Boundary conditions

$$k = \frac{2\pi n}{L}$$

$$\frac{\omega}{v} = \frac{2\pi n}{L}$$

Both lead to $\sin \frac{\pi n x}{L}$.

It must be the BC that break x, t symmetry

WE-2

Not just a Math question:

What determines the sound our ear perceives?

Does ear measure k or ω ? If k then all strings would same indep of T/μ .

Similar Q for eyes

$$c = \lambda f$$



$$\begin{array}{c} v = \lambda' f' \\ \uparrow \quad \uparrow \\ \frac{\lambda}{n} \quad f \\ n \end{array}$$

why??

What color do you see?

Q: Is it changed in medium of index n or not?

Eye is sensitive to f not λ !

Why?