

Molecular Dynamics

Galaxy formation  
 Nanoclusters (QM-force  
 classical-mass  
 nuclei)  
 ↓ Protein Folding

A powerful and widely used research tool (yet very simple)

$$v = \frac{dx}{dt} \rightarrow dx = v dt \rightarrow x = x + v dt$$

$$a = \frac{F(x,v)}{m} = \frac{dv}{dt} \rightarrow dv = \frac{F(x,v)}{m} dt \rightarrow v = v + \frac{F(x,v)}{m} dt$$

1) COPE:

1) start with  $x_0, v_0$

2) get  $x_1, v_1$

iterate (not unlike Fibonacci code)

→  $x(t), v(t)$

\*  $dt$  must be small

Slight subtlety

$$x_1 = x_0 + v_0 dt$$

$$v_1 = v_0 + \frac{F(x_0, v_0)}{m} dt$$

$$v_1 = v_0 + \frac{F(x_1, v_0)}{m} dt$$

↑  
"Euler"

↑  
"Leapfrog"

Leapfrog is much more stable

HW 1)  $F(x,v) = -Kx$  ← HW 2

2)  $= -kx - \gamma v$  ← OPTIONAL

3)  $= -kx - ax^3 - \gamma v$  ← HW 3