

$$25 - 1, 13, 28, 42, 55, 68, 84$$

$$26 - 6, 23, 25, 31, 33, 67, 84$$

$$27 - 01, 07, 012, 4, 17, 15, 40, 56, 66$$

25-1

$$I = \Delta Q / \Delta t$$

$$\Delta Q = I \Delta t = 25000 (40 \cdot 10^{-6}) = 1 \text{ C}$$

25-13

$$R = \rho L / A = (1.72 \cdot 10^{-9})^2 / \pi (.814 \cdot 10^{-3})^2 = 1.65 \cdot 10^{-3} \Omega$$

$$V = IR = (12.5 \cdot 10^{-3}) R = 2.07 \cdot 10^{-5} \text{ V}$$

Silver has $\rho = 1.47 \cdot 10^{-8}$, instead of $1.72 \cdot 10^{-8}$; same calculation

25-28

$$24 - 4r = 21.2 \text{ V}$$

$$r = 0.7 \Omega$$

$$24 - 4r - 4R = 0$$

$$R = 5.3 \Omega$$

25-42

$$P = VI = 9(1.13) = 1.17 \text{ Watts}$$

25-55

$$R = \rho L / A \rightarrow \rho = AR / L$$

$$a) \rho = \pi (1.25 \cdot 10^{-3})^2 (.104) / 14 = 3.64 \cdot 10^{-8}$$

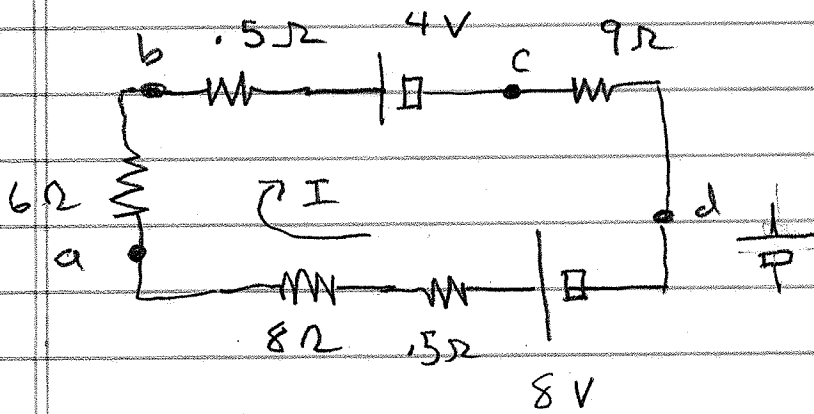
$$b) V = E_d = (1.28)(14) \quad I = V / R_0 = 17.9 / .104 = 172 \text{ Amps}$$

$$c) I = nqVA \quad v = \frac{172}{8.5 \cdot 10^{28} (1.6 \cdot 10^{-19}) \pi (1.25 \cdot 10^{-3})^2} = 2.58 \cdot 10^{-3} \text{ m/s}$$

2.

25-68

Compute I first



$$+8 - 24I - 4 = 0$$

Sum of all R

$$I = 1/6 \text{ A}$$

a) $V_d + 8 - 8.5I = V_a$ $V_a - V_d = 6.58 \text{ Volts}$

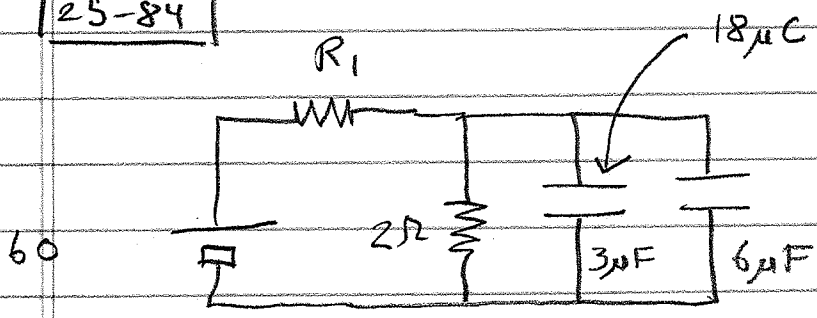
b) $V_b - .5(1/6) - 4 = V_c$ $V_b - V_c = 4.08 \text{ Volts}$

c) $+8 - 24I - 4 - 10.3 = 0$

$$I = -0.27 \text{ Amps}$$

$V_b - .5(-.27) - 4 = V_c$ $V_b - V_c = 3.86 \text{ Volts}$

25-84



Voltage across capacitors must be identical

$$C = Q/V$$

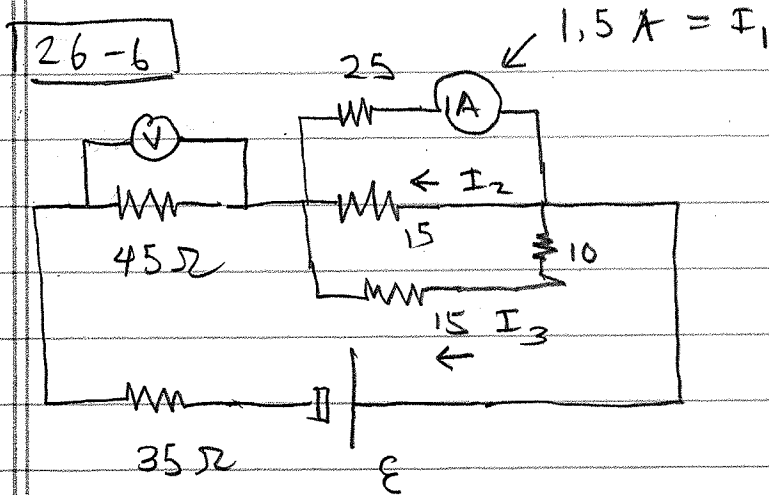
$$V = Q_1/C_1 = 18 \mu\text{C} / 3 \mu\text{F} = 6$$

$$Q_2 = C_2 V = 36 \mu\text{C}$$

Voltage across 2 ohm resistor must also be 6 volts so $I = 3 \text{ A}$

Then $60 - 3R_1 - 6 = 0$ $R_1 = 18 \Omega$

3.



$$25(1.5) = 15 I_2 = 25 I_3$$

$$I_2 = 2.5 A$$

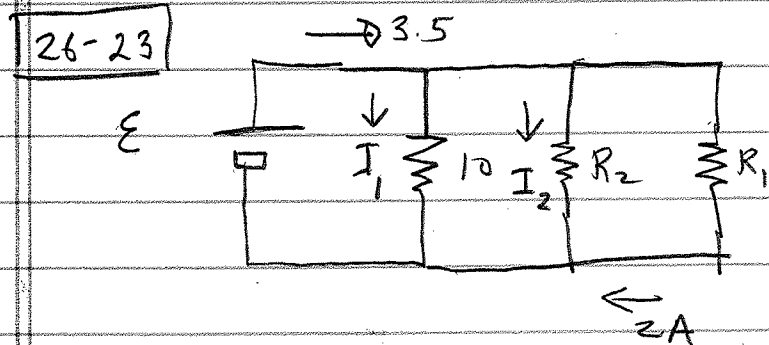
$$I_3 = 1.5 A$$

$$\text{Total current} = I_1 + I_2 + I_3 = 5.5 A$$

$$\text{Voltmeter reads } 45(5.5) = 248 \text{ Volts}$$

$$\epsilon - 25(1.5) - 248 - 35(5.5) = 0$$

$$\epsilon = 478 \text{ Volts}$$



$$3.5 = I_1 + I_2 + 2$$

$$2R_1 = I_2 R_2$$

$$\textcircled{3} \rightarrow 2R_1 = I_1 \cdot 10$$

$$\epsilon - 10I_1 = 0$$

$$R_1 = 20 \text{ ? Assume ?}$$

5 Unknowns $\epsilon, I_1, I_2, R_1, R_2$

$$I_1 = 4 A \text{ from } \textcircled{3}$$

4.

$$26.23 \text{ cont'd} \quad P = 2(20) = 40 \text{ Watts}$$

$$40 \text{ Watts} = 40 \text{ J/s} = 9.57 \text{ cal/s} \quad 1 \text{ cal} = 4.18 \text{ J}$$

$$\Delta Q = cm\Delta T = \left(1 \frac{\text{cal}}{\text{g}^\circ\text{C}}\right)(100 \text{ g})(48) = 4800 \text{ cal}$$

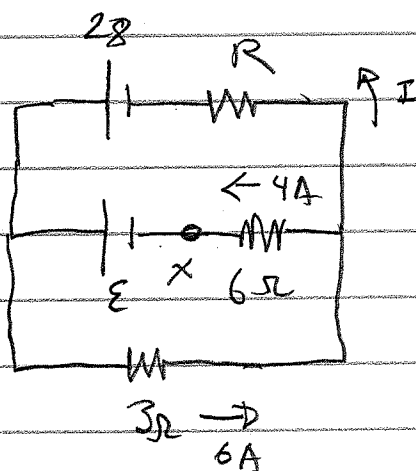
$$\Delta t = \frac{4800 \text{ cal}}{9.57 \text{ cal/sec}} = 502 \text{ sec}$$

Can also compute \mathcal{E} , I_2 , R_2 if wanted:

$$\text{From } \textcircled{1} \quad 3.5 = 4 + I_2 + 2 \quad I_2 = -2.5 \text{ A}$$

This problem doesn't make sense, at least if we assume $R_1 = 20 \Omega$.

26-25



$$\text{a) } 6 = 4 + I \\ I = 2 \text{ A}$$

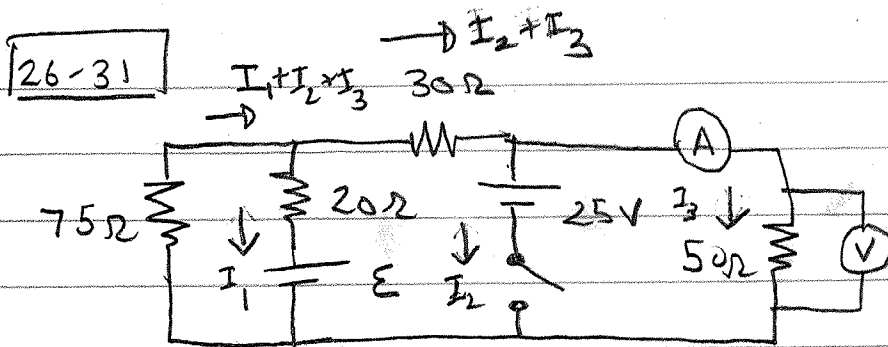
$$\text{b) } -2R + 28 - 3(6) = 0 \\ R = 5 \Omega$$

$$\text{c) } 28 - \mathcal{E} + 24 - 3(2) = 0 \\ \mathcal{E} = 42 \text{ Volts}$$

$$\text{d) } 28 - I(5) - I(3) = 0$$

$$I = 3.5 \text{ A}$$

5.



a) S open: $V = 15V \Rightarrow I_3 = 15/50 = 0.3 \text{ Amp}$
 $I_2 = 0$

$$\varepsilon + 20I_1 - 30(I_2 + I_3) - 50I_3 = 0$$

$$\varepsilon + 20I_1 - 80(0.3) = \varepsilon + 20I_1 - 24 = 0$$

$$\varepsilon + 20I_1 + 75(I_1 + I_3) = 0$$

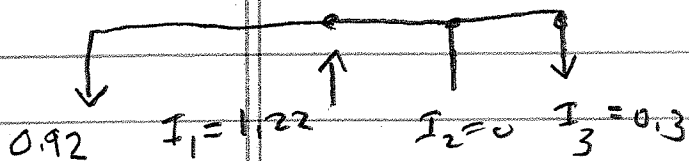
$\uparrow 0.3$

$$\varepsilon + 95I_1 + 22.5 = 0$$

$$\varepsilon + 20I_1 - 24 = 0$$

$$15I_1 + 46.5 = 0 \quad I_1 = -0.62A$$

$$\varepsilon = 36.4 \text{ V. } \uparrow$$

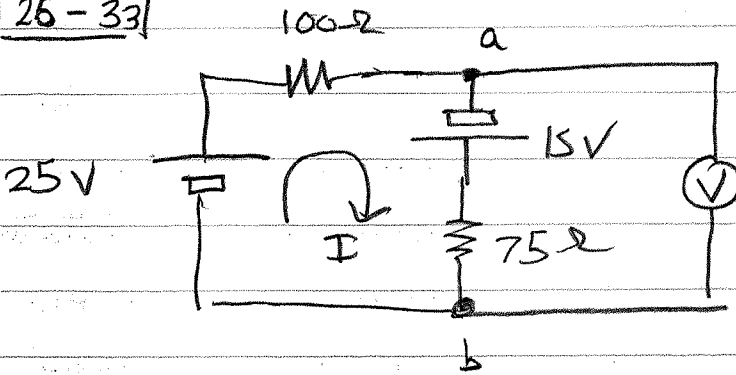


check $36.4 - 20(0.62) - 75(0.32) = 0 \checkmark$

b) $I = 25/50 = 1/2 \text{ Amp}$

6.

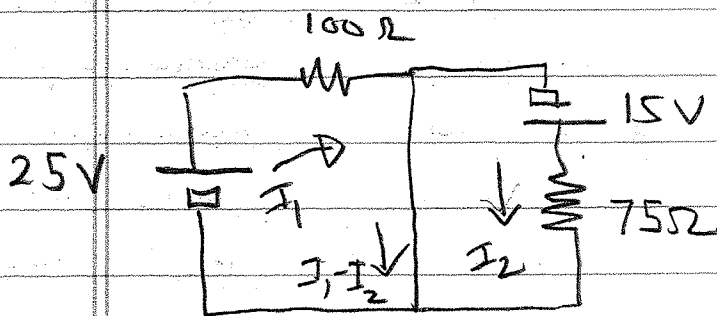
26-33



$$25 - 100I + 15 - 75I = 0 \quad I = \frac{40}{175} = 0.23 \text{ A}$$

$$V = 15 - 75(0.23) = 7.86 \text{ V}$$

b is at higher potential



$$25 - 100I_1 = 0$$

$$I_1 = 0.25 \text{ A}$$

$$15 - 75I_2 = 0$$

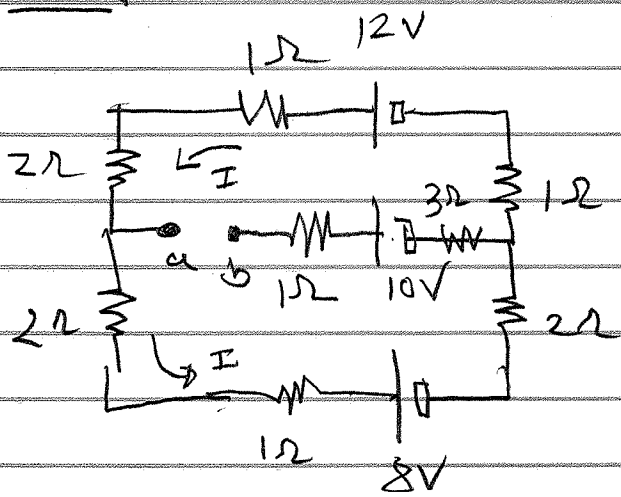
$$I_2 = 0.20 \text{ A}$$

Through switch $I_1 - I_2 = 0.05 \text{ A}$

7.

26-67

a)



$$+12 - 1I - 2I - 2I - 1I$$

$$-8 - 2I - 1I = 0$$

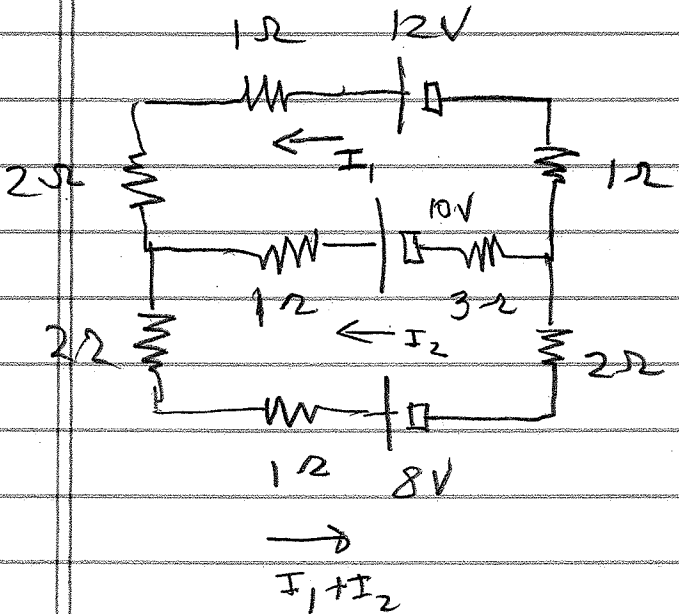
$$4 - 9I = 0$$

$$I = 4/9 \text{ A}$$

Choosing $V_b = 0$ \parallel $V_a = 0 - 1(0) - 10 - 3(0)$

$$-1(4/9) + 12 - 1(4/9) - 2(4/9) = 0$$

$$V_a = 12 - 16/9 = 2/9 \text{ Volts}$$



$$12 - I_1 - 2I_1 - 2(I_1 + I_2)$$

$$- (I_1 + I_2) - 8 - 2(I_1 + I_2)$$

$$- I_1 = 0$$

$$4 - 9I_1 - 5I_2 = 0$$

$$12 - I_1 - 2I_1 + I_2 - 10 + 3I_2$$

$$- I_1 = 0$$

$$2 - 4I_1 + 4I_2 = 0$$

2 2
4 5

$$4 - 9I_1 - 5I_2 = 0$$

$$1 - 2I_1 + 2I_2 = 0$$

$$13 - 28I_1 = 0$$

$$I_1 = 13/28 \quad I_2 = -1/28$$

$$-1 - 28I_2 = 0$$

8.

$$\boxed{25-84} \quad a) \quad U = \frac{Q^2}{2C} = \frac{(6.9 \cdot 10^{-3})^2}{2(4.62 \cdot 10^{-6})}$$

$$= 5.15 \text{ J}$$

$$Q(t) = Q_0 e^{-t/RC} \quad I(t) = -\frac{Q_0}{RC} e^{-t/RC}$$

$$b) \quad P_0 = I_0 V_0 = \frac{(6.9 \cdot 10^{-3})^2}{850(4.62 \cdot 10^{-6})^2} = 2624 \text{ watts}$$

$$\begin{array}{cc} \nearrow & \nearrow \\ \frac{Q_0}{RC} & \frac{Q_0}{C} \end{array}$$

c) If U is $1/2$ its initial value the charge must be $1/\sqrt{2}$ of Q_0 , i.e. $e^{-t/RC} = 1/\sqrt{2}$

$$P = |IV| = \frac{1}{RC} Q_0 e^{-t/RC} \frac{Q_0 e^{-t/RC}}{C} = \frac{Q_0^2}{RC^2} (e^{-t/RC})^2$$

\uparrow
 $1/2$

So power is $1/2$ that in part (b), 1312 watts.

Notice that total energy dissipated in resistor is

$$U_{\text{lost}} = \int_0^{\infty} P dt = \int_0^{\infty} |IV| dt = \int_0^{\infty} \frac{Q_0^2}{RC^2} e^{-2t/RC} dt$$

$$= \frac{Q_0^2}{RC^2} \int_0^{\infty} e^{-2t/RC} dt = \frac{Q_0^2}{RC^2} \frac{RC}{2} = \frac{Q_0^2}{2C}$$

$$= \frac{RC}{2} e^{-2t/RC} \Big|_0^{\infty} = U_0$$

9.

$$\boxed{27-01} \quad \text{Since } \vec{F} = q \vec{v} \times \vec{B}$$

$$|\vec{F}| = q |\vec{v}| |\vec{B}| \sin \theta$$

↖ angle between \vec{v} and \vec{B}

$$\text{If } \vec{v} \parallel \vec{B} \quad \theta = 0 \quad \text{and} \quad |\vec{F}| = 0$$

so, yes, there can be no force if $\vec{v} \parallel \vec{B}$

$$\boxed{27-07} \quad F_{\text{tot}} = q \vec{E} + q \vec{v} \times \vec{B} = m \vec{a}$$

$$\text{if } \vec{v} = \text{constant} \quad \vec{a} = 0 \quad \text{so} \quad \vec{E} + \vec{v} \times \vec{B} = 0$$

$$\text{If } \vec{B} = 0 \quad \text{we conclude } \vec{E} = 0$$

$$\text{However if } \vec{E} = 0 \quad \text{all we can say is } \vec{v} \times \vec{B} = 0$$

see Q1.

$$\boxed{27-012} \quad \text{a) } q \vec{v} \times \vec{B} = q v_0 \hat{y} \times B_0 \hat{x} = -q v_0 B_0 \hat{z}$$

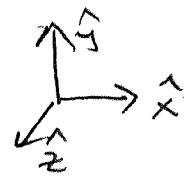
$$\text{b) } q \vec{v} \times \vec{B} = q v_0 \hat{z} \times B_0 \hat{x} = q v_0 B_0 \hat{y}$$

$$\text{c) } q \vec{v} \times \vec{B} = -q v_0 \hat{x} \times B_0 \hat{x} = \phi$$

$$\text{d) } q \vec{v} \times \vec{B} = q v_0 \frac{1}{\sqrt{2}} (\hat{x} - \hat{z}) \times B_0 \hat{x} = -q v_0 B_0 / \sqrt{2} \hat{y}$$

$$\text{e) } q \vec{v} \times \vec{B} = q v_0 \frac{1}{\sqrt{2}} (\hat{y} - \hat{z}) \times B_0 \hat{x} = \frac{q v_0 B_0}{\sqrt{2}} (-\hat{z} - \hat{x})$$

10.



$$\boxed{27-4} \quad \vec{a} = \vec{F}/m = q \vec{v} \times \vec{B} / m$$

$$= \frac{1.22 \cdot 10^{-8}}{181 \cdot 10^{-3}} \left(3 \cdot 10^4 \hat{y} \times (1.63 \hat{x} + 0.980 \hat{y}) \right)$$

$$\hat{y} \times \hat{x} = -\hat{z} \quad \hat{y} \times \hat{y} = 0$$

$$= -0.33 \hat{z} \text{ m/s}^2$$

$$\boxed{27-14} \quad \phi_B = |\vec{B}| A \cos \theta \quad \text{if } \vec{B} \text{ is uniform}$$

\uparrow
angle between
normal to surface
and \vec{B}

$$a) \quad \phi_B = (0.128)(1.3)(1.4) \cdot \cos 90^\circ = 0$$

$$\left\{ \begin{array}{l} \hat{n} = \hat{x} \perp B \hat{z} \end{array} \right.$$

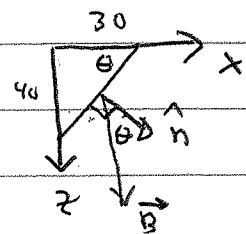
$$b) \quad \phi_B = (0.128)(1.3)(1.3) \cdot \cos 180^\circ = -.115 \text{ T} \cdot \text{m}^2$$

Δ use outward normal $\hat{n} = -\hat{z}$

$$c) \quad \phi_B = (0.128)(1.3)(1.5) \cos \theta$$

$$\left\{ \begin{array}{l} \uparrow \\ 3/5 \end{array} \right.$$

$$= +.115 \text{ Tm}^2$$



$$d) \quad \text{flux through abc and def} = 0 \text{ since } \hat{n} = \hat{y} \perp \vec{B}$$

Total flux = 0 .

11

↙ circular motion $a = v^2/r$

27-15

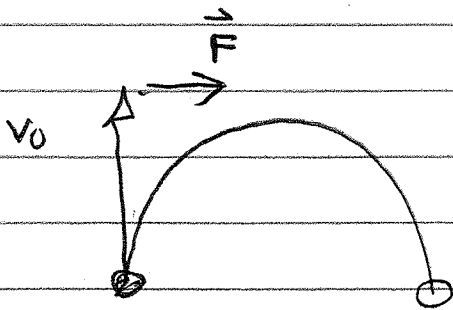
a)

$$mv^2/r = \underbrace{qVB}_{F_{\text{mag}}}$$

$$B = \frac{mv^2}{qr} = \frac{(9.11 \cdot 10^{-31})(1.41 \cdot 10^6)^2}{(1.6 \cdot 10^{-19})(0.1)} = 8.10 \cdot 10^{-5} \text{ T}$$

$$= 0.8 \text{ Gauss}$$

want force to right, so \vec{B} must be out



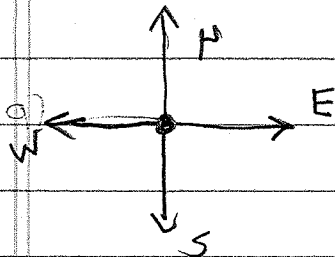
of paper.

$$b) T = 2\pi r/v = 2\pi(0.1)/1.41 \cdot 10^6 = 4.46 \cdot 10^{-7} \text{ sec}$$

27-40

$$|\vec{F}| = I l B \sin \theta$$

↑ angle between wire and B



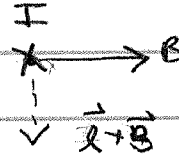
I is into paper ("downward")

In all a, b, c $\theta = 90^\circ$ so $\sin \theta = 1$

$$|\vec{F}| = \underbrace{(1.2)}_I \underbrace{(0.01)}_l \underbrace{(0.588)}_B = 7.06 \cdot 10^{-3} \text{ N}$$

27-40 cont'd

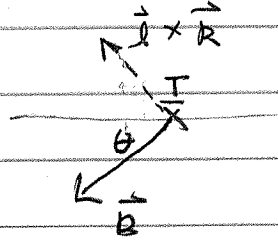
a) direction is South



b) direction is West



c) direction is



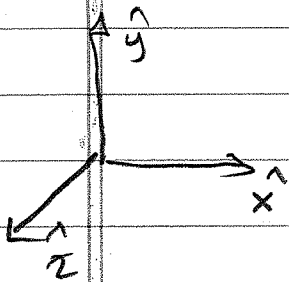
60° N of West.

27-56

$$q \vec{v} \times \vec{B}$$

$$= (9.45 \cdot 10^{-8}) (-1.68 \cdot 10^4 \hat{x} - 3.11 \cdot 10^4 \hat{y} + 585 \cdot 10^4 \hat{z})$$

$$\times 0.65 \hat{x}$$



$$\hat{x} \times \hat{x} = 0$$

$$\hat{y} \times \hat{x} = -\hat{z}$$

$$\hat{z} \times \hat{x} = +\hat{y}$$

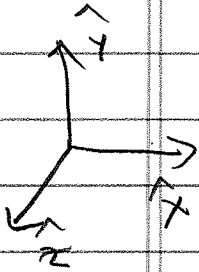
$$= 1.91 \cdot 10^{-3} \hat{z} + 3.60 \cdot 10^{-3} \hat{y}$$

13.

27-66

$$\vec{F} = F_0(3\hat{x} + 4\hat{y})$$

$$\vec{v} = v\hat{z}$$



$$3F_0\hat{x} + 4F_0\hat{y} = q v\hat{z} \times (B_x\hat{x} + B_y\hat{y} + B_z\hat{z})$$

$$= qv(B_x\hat{y} - B_y\hat{x})$$

a) We see $B_x = 4F_0/qv$

$$B_y = -3F_0/qv$$

We get no information about B_z .

b) $|B|^2 = \frac{36F_0^2}{q^2v^2} = B_x^2 + B_y^2 + B_z^2$

$$= \frac{F_0^2}{q^2v^2} \{16 + 9\} + B_z^2$$

$$B_z^2 = 11F_0^2/q^2v^2$$

We cannot tell sign of B_z