Instructions: This examination is closed book. Only a calculator is allowed. Show all your work. Credit will only be given for complete solutions. All questions are worth the same number of points.

Some facts: The specific heat of ice is 2100 J/(kg K).
The latent heat of fusion of water is 334 x 10³ J/kg.
The latent heat of vaporization of water is 2256 x 10³ J/kg.
The ideal gas law constant R=8.314 J/(mole K).

(1) Three moles of a monatomic ideal gas go through the cycle abc. For the complete cycle, 600 J of heat flow out of the gas. Process ab is at constant pressure, and process bc is at constant volume. States a and b have temperatures $T_a = 240K$ and $T_b = 360K$.
(a) Sketch the pV-diagram. Explain the reasoning behind the particular cycle trajectory you draw.
(b) What is the work $W$ for the process ca?

\[ a) \text{ Since process is cyclic } \Delta U = 0 \implies W = Q. \text{ If } 600 \text{ J flow out, } Q = -600 \text{ J} \]

So $W = -600 \text{ J}$. This means the path where V decreases must be above the path where V increases. Also, since $T_b > T_a$ and $P_b = P_a$, $V_b > V_a$.

\[ b) \quad W = -600 = W_{ab} + W_{bc} + W_{ca} \]

Useful together, but not separately:
\[ \Delta U_{ab} = nC_v \Delta T = 3 \left( \frac{3}{2} \right) \left( 8 \cdot 314 \right) (120) = 44,900 \text{ J} \]
\[ \Delta U_{cb} = nC_p \Delta T = 3 \left( \frac{5}{2} \right) \left( 8 \cdot 314 \right) (120) = 74,833 \text{ J} \]

Since process ab is not a cycle $\Delta U_{ab} \neq 0$. Instead:
\[ W_{ab} = (Q_{ab} - \Delta U_{ab}) \]

The easier way:
\[ W_{ab} = P \Delta V = \frac{nRT}{V_a} - \frac{nRT}{V_b} = nRT \left( \frac{V_b - V_a}{V_b V_a} \right) = 3(8 \cdot 314)(120) = 2,983 \text{ J} \]

\[ W_{ca} = -600 - W_{ab} = -600 - 2,983 = -3,593 \text{ J} \]

(2) An open container holds 0.750 kg of ice at -20°C. The mass of the container can be ignored. Heat is supplied to the container at a constant rate of 1100 J/min.
(a) After how many minutes does the ice begin to melt?
(b) After how many minutes, from the time the heating is first started, does the temperature begin to rise above 0°C?

(a) To raise ice 20° from -20° to 0° requires
\[ Q = m C \Delta T = 0.75 \cdot (2100)(20) = 31,500 \text{ J} \]

at 1100 J/min we need 28.6 mins

(b) To melt ice requires
\[ Q = mL_f = 0.75 \cdot (334 \cdot 10³) = 250,500 \text{ J} \]

at 1100 J/min this means 228 minutes more

so it rises above 0°C at 28.6 + 228 = 256 min
A carpenter builds an exterior house wall with a layer of wood 4.0 cm thick on the outside, and a layer of Styrofoam 3.0 cm thick on the inside wall surface. The wood has $k = 0.070 \text{ W/(m K)}$ and the Styrofoam has $k = 0.008 \text{ W/(m K)}$. The interior surface temperature is $20^\circ \text{C}$ and the exterior surface temperature is $-12^\circ \text{C}$. What is the temperature at the plane where the wood meets the Styrofoam? What is the rate of heat flow per square meter through this wall?

(a) Heat flow is $kA \Delta T/e$. Assuming transients have settled down, the flow through the wood and styrofoam must be equal:

$$
(0.07) A \frac{(T_m - (-12))}{0.4} = \frac{0.008 A (20 - T_m)}{0.3}
$$

$$
1.75T_m + 21 = 5.33 - 0.27T_m
$$

$$
T_m = -7.76^\circ \text{C} \implies 262.24^\circ \text{K}
$$

(b) Heat flow $= \frac{0.008}{0.3} A (20 - (-7.76)) = 7.40 A$

$\Rightarrow 7.40 \text{ Watts/m}^2$

At what temperature is the root-mean-square speed of nitrogen molecules equal to the root-mean-square speed of hydrogen molecules at $30^\circ \text{C}$? The molar mass of hydrogen is $1.008 \text{ g}$ and the molar mass of nitrogen is $14.007 \text{ g}$.

$$
V_{rms} = \left(\frac{\frac{3}{2} k_B T}{m}\right)^{1/2}
$$

$$
\left(\frac{3}{2} k_B T_N_2 / m_{N_2}\right)^{1/2} = \left(\frac{3}{2} k_B T_{H_2} / m_{H_2}\right)^{1/2}
$$

$$
\Rightarrow T_{N_2} = \frac{m_{N_2}}{m_{H_2}} T_{H_2} = \frac{14.007}{1.008} \frac{303^\circ \text{K}}{1.008}
$$

$$
= 4210^\circ \text{K} \implies 3937^\circ \text{C}
$$
[b] Answer two of the following questions. Your answers must be complete and clear. If you respond to more than two, the grader will mark the first ones he sees.
(a) An ideal gas is expanding (volume increasing). Does the pressure fall faster if the expansion is adiabatic or if it is isothermal? Why?
(b) Explain the difference between $C_p$ and $C_V$. Which is bigger? Why?
(c) What is the 'equipartition theorem'? How do you use it to get $C_V$ for a monatomic gas? What about a diatomic gas?
(d) What does each of the letters in $r_{rms}$ stand for? Why do we use $v_{rms}$ to describe how a bunch of molecules are moving instead of just talking about the average velocity?

(a) In adiabatic expansion no heat enters while the gas does work, hence $\Delta U < 0$ and $T$ is falling. So $T$ is lower for adiabatic expansion than isothermal. A lower pressure results.
This can also be seen by comparing eqns $P = \frac{c}{V}$ (isothermal) and $P = \frac{c}{\sqrt{V}}$ (adiabatic).

(b) $C_p$ and $C_V$ are specific heats at constant pressure and volume respectively. For a given rise in temperature $\Delta T$ more heat is needed if gas expands since it is doing work. Thus at constant $P$, where gas expands $C = \frac{\Delta Q}{\Delta T}$ is larger than at constant volume.

(c) Every term like $\frac{1}{2} m v_x^2$, $\frac{1}{2} m v_y^2$, ... to internal energy gives a contribution $\frac{1}{2} k_B$ to specific heat. For monatomic gas we just have $\frac{1}{2} m (v_x^2 + v_y^2 + v_z^2) \Rightarrow C_V = \frac{3}{2} k_B$. But diatomic gas has $\frac{1}{2} k_B v_x^2$ and $\frac{1}{2} k_B v_z^2 \Rightarrow C_V = \frac{5}{2} k_B$.

(d) $r_{rms} = \text{root-mean-square}$. Average velocity of molecule changes "distance" to "displacement" or "position".

[6] One afternoon while very bored you decide to play a game where you flip a fair coin and move one meter to the right if you get 'heads' and one meter to the left if you get 'tails'. What are the possible distances you can be from your starting point after you toss the coin and move four times? What are the probabilities that you will be at those distances? Explain your reasoning.
Answer **two** of the following questions. Your answers must be complete and clear. If you respond to more than two, the grader will mark the first ones he sees.

(a) How many Joules are there in a kilowatt-hour? How much does PGE charge you for a kilowatt-hour of electricity? (You will be marked correct if your answer about PGE rates is within a factor of three of the correct one.)

(b) Give two ways temperature is measured. What is the physical property that is changing in each case?

(c) Usually when you add heat to a material its temperature goes up. Name two situations where the temperature goes not increase. Where is the heat energy going?

(d) Why the heck did this numbskull put a long crack in the sidewalk he’s building?

(a) \[ \text{KW-hour} = 1000 \frac{\text{J}}{\text{sec}} \times 3600 \text{ sec} = 3.6 \times 10^6 \text{ J} \]

PGE charges about \( 20 \) \( c \) for a kw-hr of electricity.

(b) \( T \) can be measured with a mercury thermometer. The volume of mercury changes with \( T \).

\( T \) can also be measured by monitoring the change of electrical resistance with \( T \).

(c) When a material is changing from solid to liquid or liquid to gas its temperature stays fixed. The heat goes into breaking bonds between atoms.

(d) The builder knows \( \Delta L = L_0 \Delta T \) so that when \( T \) goes up his concrete will expand. Without the expansion joint, it will crack.