

P9B FALL 2013

ASSIGNMENT 3

16- 3, 6, 25, 33, 37, 45, 73

16-3

The relation between pressure amplitude and displacement amplitude is:

$$P = BkA$$

pressure amplitude \rightarrow P
Bulk modulus \rightarrow B
displacement amplitude \rightarrow A
wave number \rightarrow k

Here $A = .02 \text{ mm}$

$$f = 150 \text{ Hz}, 1500 \text{ Hz}, 15000 \text{ Hz}$$

$$v_{\text{sound}} = 344 \text{ m/s}$$

$$B = 1.42 \cdot 10^5 \text{ Pa}$$

a) $\lambda f = v \quad \lambda = \frac{344}{150} = 2.29 \text{ m}$
 $k = 2\pi/\lambda = 2.74 \text{ m}^{-1}$

$$P = BkA = 1.42 \cdot 10^5 \text{ Pa} (2.74) (.02 \cdot 10^{-3}) = 7.78 \text{ Pa}$$

< PAIN THRESHOLD

b) $f = 1500 \rightarrow \lambda = 1/10 \text{ as in (a)}$

$$\rightarrow k = 10 \times \text{as in (a)} \rightarrow P = 77.8 \text{ Pa} > \text{PAIN}$$

c) $f = 15000 \quad P = 778 \text{ Pa} > \text{PAIN}$

16-6

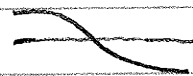
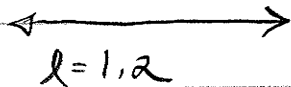
a) $v = \sqrt{B/\rho} \rightarrow B = \rho v^2 = (1300) \left((400)8 \right)^2 = 1,33 \cdot 10^{10} \text{ Pa}$
 \uparrow
 $f\lambda$

b) $v = \sqrt{Y/\rho} \rightarrow Y = \rho v^2 = 6400 (3846)^2 = 9,47 \cdot 10^{10} \text{ Pa}$

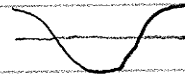
$v = l/t = 1,5 / 3,9 \cdot 10^{-4} = 3846$

16-25

A) OPEN BOTH ENDS



$1/2 \lambda = l$



$\lambda = l$

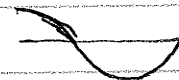


$3/2 \lambda = l$

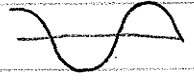
B) CLOSED ONE END



$1/4 \lambda = l$



$3/4 \lambda = l$



$5/4 \lambda = l$

	DISPLACEMENT NODES	$x = 0,6$	$x = 0,3, 0,9$	$x = 0,2, 0,6, 1,0$
A)	PRESSURE NODES	$x = 0, 1,2$	$x = 0, 0,6, 1,2$	$x = 0, 0,4, 0,8, 1,2$
B)	DISPLACEMENT NODES	$x = 1,2$	$x = 0,4, 1,2$	$x = 0,24, 0,72, 1,2$
	PRESSURE NODES	$x = 0$	$x = 0, 0,8$	$x = 0, 0,48, 0,96$

3.

16-33 a) For constructive interference the extra distance traveled from A must be an integer # of wavelengths

$$d = n\lambda$$

↑

extra distance

$$\lambda = 2/n$$

lowest frequency

⇒ largest λ so $n=1$

$$\lambda = 2 \text{ m}$$

$$\lambda f = v = 344$$

$$a) f = 172 \text{ sec}^{-1}$$

b) Destructive interference

$$d = \frac{1}{2}\lambda, \frac{3}{2}\lambda, \dots$$

again largest λ gives lowest f

$$\lambda_{\text{max}} = 4$$

$$\lambda f = v = 344$$

$$b) f = 86 \text{ sec}^{-1}$$

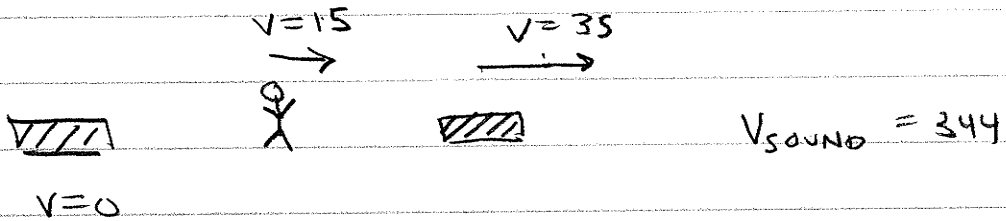
16-37 The difference in distance is 1.4 m

$$\text{The wavelength } \lambda = v/f = 344/860 = 0.4 \text{ m}$$

Distance difference is $\frac{7}{2}\lambda \rightarrow$ destructive.

16-45

$$f = 392 \text{ Hz}$$



$$\begin{aligned}
 \text{a)} \quad f' &= 392 \frac{344 - 15}{344} = 375.4 \text{ Hz} \\
 \text{b)} \quad f' &= 392 \frac{344 + 15}{344 + 35} = 371.2 \text{ Hz}
 \end{aligned}
 \quad \left. \vphantom{\begin{aligned} \text{a)} \\ \text{b)} \end{aligned}} \right\} \text{ Beat} = 4.4 \text{ Hz}$$

35 15

16-73

$$\frac{1}{2} m v^2 = m g h$$

$$v = \sqrt{2gh} = 49.5 \text{ m/s}$$

\nearrow
 9.8 125

$$\text{a)} \quad f = 2500 \frac{344 - 49.5}{344 + 49.5} = 2186 \text{ Hz}$$

$$\text{b)} \quad f = 2500 \frac{344 + 49.5}{344 - 49.5} = 2920 \text{ Hz}$$