

**PHYSICS 102**  
**CLASSICAL MECHANICS LAB**  
**FALL 2013**

**Assignment Three**

**Due Wednesday, October 30, 7:00 pm.**

- [1.] Write a code to iterate  $x_{n+1} = 1 - \mu x_n^2$ . Print it and hand it in.
- [2a.] Run your code for  $\mu = 0.5$  and the three initial values  $x_0 = 0.25, 0.50, 0.75$ . What happens?
- [2b.] Compute the fixed point of the map analytically and show your code is doing the right thing.
- [3a.] Run your code for  $\mu = 1.1$  and the three initial values  $x_0 = 0.25, 0.50, 0.75$ . What happens?
- [3b.] Compute the fixed points of the twice-iterated map analytically and show your code is doing the right thing.
- [4.] Run your code for  $\mu = 1.3$  and the initial value  $x_0 = 0.25$ . What happens?
- [5.] Run your code for  $\mu = 1.5$  and the initial value  $x_0 = 0.25$ . What happens?
- [6.] Make plots of  $x(n)$  vs  $n$  for  $x_0 = 0.25$  and the four  $\mu$  values above.
- [7.] Extra Credit! Do a ‘stability analysis’ of the fixed point and show that it goes unstable at  $\mu = 0.75$ . I can discuss this in more detail with you, but the idea is to start  $x_0$  at a value slightly shifted from the fixed point and decide whether the deviation increases or decreases after an iteration.