

PHYSICS 102
CLASSICAL MECHANICS LAB
FALL 2015

Assignment Three

Due Wednesday, October 28, 7:00 pm.

- [1.] Write a code to iterate $x_{n+1} = 1 - \mu x_n^2$. Print it and hand it in.
- [2a.] Run your code for $\mu = 0.5$ and the three initial values $x_0 = 0.25, 0.50, 0.75$. What happens?
- [2b.] Compute the fixed point of the map analytically and show your code is doing the right thing.
- [3a.] Run your code for $\mu = 1.1$ and the three initial values $x_0 = 0.25, 0.50, 0.75$. What happens?
- [3b.] Compute the fixed points of the twice-iterated map analytically and show your code is doing the right thing.
- [4.] Run your code for $\mu = 1.3$ and the initial value $x_0 = 0.25$. What happens?
- [5.] Run your code for $\mu = 1.5$ and the initial value $x_0 = 0.25$. What happens?
- [6.] Make plots of $x(n)$ vs n for $x_0 = 0.25$ and the four μ values above.
- [7.] Extra Credit! Do a ‘stability analysis’ of the fixed point and show that it goes unstable at $\mu = 0.75$. I can discuss this in more detail with you, but the idea is to start x_0 at a value slightly shifted from the fixed point and decide whether the deviation increases or decreases after an iteration.